

# Principi programskih jezikov

## Aritmetični izrazi

Cela števila : + x spremenljivke

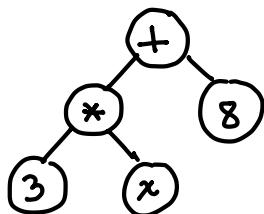
x ima vrednost 7

$$3 \times x + 8 \rightsquigarrow 29$$

### Sintaksa

Konkretna : "3 \* x + 8" niz znakov

Abstraktna : drevo

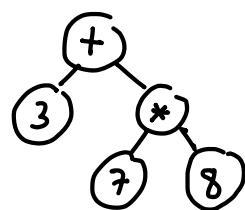
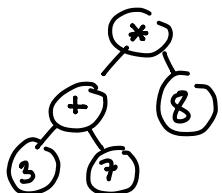


Konkretna RPN

3 7 + 8 \*

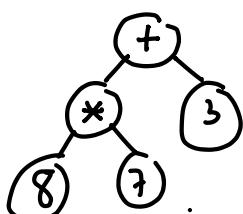
3 7 8 \* +

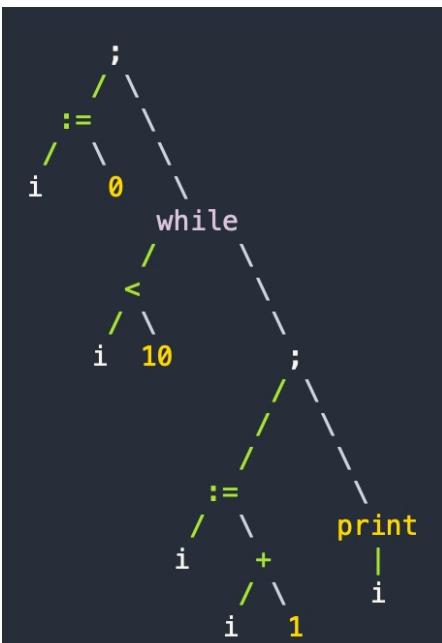
$$3 + 7 * 8 \xrightarrow{(3+7)*8} 3 + (7 \times 8)$$



"8 \* 7 + 3"

"59"

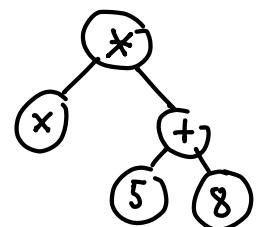
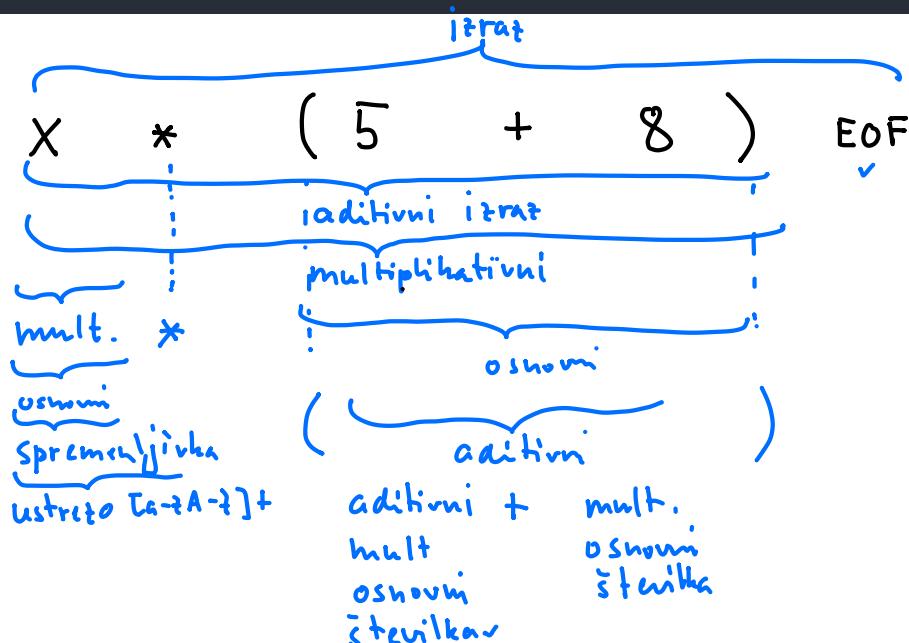




```
i := 0 ;  
while i < 10:  
    i := i + 1 ;  
    print i
```

```
i = 0;  
while (i < 10) {  
    i = i + 1;  
    System.out.println(i);  
}
```

```
(izraz) ::= <aditivni-izraz> EOF
<aditivni-izraz> ::= <multiplikativni-izraz> | <aditivni-izraz> + <multiplikativni-izraz>
<multiplikativni-izraz> ::= <osnovni-izraz> | <multiplikativni-izraz> * <osnovni-izraz>
<osnovni-izraz> ::= <spremenljivka> | <številka> | ( <aditivni-izraz> )
<spremenljivka> ::= [a-zA-Z]*
<številka> ::= -? [0-9]+
```

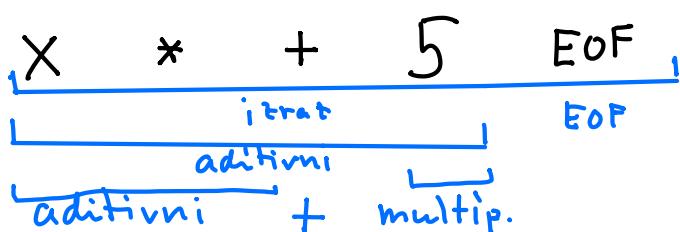


$$(x * (5 + 8))$$

```

(izraz) ::= (aditivni-izraz) EOF
(aditivni-izraz) ::= (multiplikativni-izraz) | (aditivni-izraz) + (multiplikativni-izraz)
(multiplikativni-izraz) ::= (osnovni-izraz) | (multiplikativni-izraz) * (osnovni-izraz)
(osnovni-izraz) ::= (spremenljivka) | (številka) | ( (aditivni-izraz) )
(spremenljivka) ::= [a-zA-Z] +
(številka) ::= -? [0-9] +

```



multip.  
osnovni  
· ?!

osnovni  
številka  
✓

if <pogoj>  
<ukazi> ??  
<ukazi>  
else

# Dinamična Semantika

$\alpha \beta \gamma \delta \lambda$   
 $\theta \rightarrow \{ \zeta \xi \}$   
theta zeta kesi

$$x + 3 * (y + 8)$$

Vrednosti spremenljivk:

$$\eta = [x \mapsto 2, y \mapsto 10] \quad \text{okolje}$$

↑ eta

$$[x \mapsto 2, z \mapsto 10]$$

$$\eta(x) = 2$$

$$\eta(y) = 10$$

$$\eta(z) \quad ?!$$

"v okolju  $\eta$   
se izračuna  
evalvira / vrednosti v  
število n"

Relacija:

$$\eta \mid e \hookrightarrow n$$

↑      ↑      ↑  
okolje    izraz    vrednost

$$[x \mapsto 3, y \mapsto 5] \mid 3 + x \hookrightarrow 6 \quad \checkmark$$

$$[x \mapsto 3] \mid 3 + x \hookrightarrow 17 \quad \times$$

$$[] \mid 3 + 8 \hookrightarrow 22 \quad \times$$

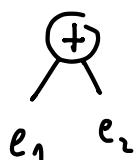
$$[x \mapsto 3] \mid 3 + z \hookrightarrow 17 \quad \times$$

$$\frac{\eta \models e_1 \hookrightarrow n_1 \quad \eta \models e_2 \hookrightarrow n_2 \quad n_1 \cdot n_2 = n}{\eta \models e_1 * e_2 \hookrightarrow n}$$

matematična operacija  
množenje

$$\boxed{\begin{array}{c} e_1 \hookrightarrow n_1 \quad \eta \models e_2 \hookrightarrow n_2 \quad n_1 + n_2 = n \\ \hline \eta \models e_1 + e_2 \hookrightarrow n \end{array}}$$

seštevanje



izpeljava

$$\frac{\frac{[x \mapsto 3](x) = 3}{[x \mapsto 3] \mid x \hookrightarrow 3} \quad \frac{\frac{[x \mapsto 3] \mid 3 \hookrightarrow 3}{[x \mapsto 3] \mid 3 * 7 \hookrightarrow 21} \quad \frac{[x \mapsto 3] \mid 7 \hookrightarrow 7}{3 + 21 = 24}}{3 \cdot 7 = 21}$$

Semantika malih korakov:

$$3 * 7 + 8 * 5 \rightarrow$$

$$21 + 8 * 5 \rightarrow$$

$$\begin{array}{r} 24 \\ + \ 40 \\ \hline 64 \end{array}$$